

**UNIVERSITY OF LONDON**

**GOLDSMITHS COLLEGE**

**B.Sc. Examination 2015**

**DEPARTMENT OF COMPUTING**

**IS53011A Language Design and Implementation**

Duration: 2 hours 15 minutes

Date and time: Monday 12 January, 2.30pm

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*There are five questions on this paper. You should answer no more than **THREE** questions. Full marks will be awarded for complete answers to a total of **THREE** questions. Each question carries 25 marks. The marks for each part of a question are indicated at the end of the part in [.] brackets.*

*There are 75 marks available on this paper.*

**THIS PAPER MUST NOT BE REMOVED FROM THE EXAMINATION  
ROOM**

**Question 1.**

- a) Define the notion of a regular expression over a given alphabet. [5]
- b) Explain briefly which kind of programming language constructs can not be described by regular expressions, and reason whether these constructs can be specified using context-free grammars. [4]
- c) Rewrite the following regular expression in a more compact format:  $(b^*c^*)^*$ . [5]
- d) Demonstrate elimination of immediate left recursion from the following context-free grammar: [6]
- (1)  $S \rightarrow SE$
  - (2)  $S \rightarrow SSa$
  - (3)  $S \rightarrow ES$
  - (4)  $S \rightarrow b$
- e) Give the algorithm for construction of predictive parsing tables. [5]

**Question 2.**

a) Consider the following grammar:  $c^* (bcc^*)^* (b | \epsilon)$ . For each of the following strings, say whether it could be generated by the grammar:

- i)  $\epsilon$
- ii) ccbccbbc
- iii) bccbccc

**[3]**

b) Develop a nondeterministic finite state automaton (NFA) for the simple language defined by the regular expression:  $ca(a|c)b$  using the Thompson's construction algorithm. **[6]**

c) Convert the NFA from part (b) above to a deterministic finite-state automaton (DFA) using the subset construction algorithm. **[12]**

d) Create the transition graph of the constructed DFA from part (c). **[4]**



**Question 3.**

a) What are the three main advantages of the LR parsing technique? [5]

b) Let the following LR grammar suitable for top-down parsing be given:

- (1)  $E \rightarrow T$
- (2)  $T \rightarrow bTc$
- (3)  $T \rightarrow bc$

i) Derive the canonical collection of items for this grammar using the sets-of-items construction algorithm. [6]

ii) Construct the DFA whose states are these sets of valid items. [4]

iii) Interpret the operation of the LR parsing algorithm on the input:  $bbccc \$$ , and show the contents of the stack, the input and the output. [10]

State	Action			Goto
	$b$	$c$	$\$$	$T$
0	$s1$			3
1	$s1$	$s4$		2
2		$s5$		
3			<i>accept</i>	
4	$r3$	$r3$	$r3$	
5	$r2$	$r2$	$r2$	

**Question 4.**

- a) Describe briefly the main four components of a context-free grammar. [4]
- b) Give a definition of grammar derivations in context of programming language compilers. [3]
- c) Consider the following LL(*l*) grammar for top-down parsing:

$$\begin{aligned}
 E &\rightarrow TF \\
 T &\rightarrow \mathbf{double} D \mid ( E ) \\
 F &\rightarrow + E \mid \epsilon \\
 D &\rightarrow * T \mid \epsilon
 \end{aligned}$$

- i) Derive the functions *FIRST* and *FOLLOW* necessary for building the corresponding parsing table for a top-down nonrecursive predictive parsing algorithm. [8]
- ii) Assume that the following parsing table for the LL(*l*) grammar from part (c) is given:

	<b>double</b>	+	*	(	)	\$
<i>E</i>	$E \rightarrow TF$			$E \rightarrow TF$		
<i>T</i>	$T \rightarrow \mathbf{double} D$			$T \rightarrow (E)$		
<i>F</i>		$F \rightarrow +E$			$F \rightarrow \epsilon$	$F \rightarrow \epsilon$
<i>D</i>		$D \rightarrow \epsilon$	$D \rightarrow *T$		$D \rightarrow \epsilon$	$D \rightarrow \epsilon$

Using this parsing table show the stack, the input and the output of the nonrecursive predictive parsing algorithm on the input string: **double \* double .** [10]

### Question 5.

- a) i) What are the two most important properties that an optimising compiler should provide? **[4]**
- ii) Explain briefly where the name “three-address code” in the field of computer programming language design comes from? **[3]**
- b) Consider the following simple function which iteratively performs summation of multiplied consecutive integers from a given array:

```
int Summation( int a[], int N )
{
    int j, sum;
    j = 1; sum = 0;
    while ( j < N )
    {
        sum = sum + a[ j-1 ] * a[ j ];
        j = j + 1;
    }
    return sum;
}
```

- i) Develop three-address intermediate code from this simple function. **[13]**
- ii) Optimise the developed three-address code using the techniques code motion and reduction in strength. **[5]**