

**UNIVERSITY OF LONDON**

**GOLDSMITHS COLLEGE**

**B. Sc. Examination 2003**

**COMPUTING AND INFORMATION SYSTEMS**

**IS52006A (CIS212)**

**Programming: Advanced Topics and Techniques**

**Duration: 3 hours**

**Date and time:**

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*Answer SIX questions.*

*Full marks will be awarded for complete answers to SIX questions.*

*You must answer THREE questions from section A and THREE questions from section B. You must answer at least ONE question on Prolog in Section B.*

*There are 150 marks on this paper.*

*Electronic calculator may be used. The make and model should be specified on the script and the calculator must not be programmed prior to the examination.*

## Section B

### Question 6

(a) Express the following lists in terms of `::` and `nil` in Standard ML.

- (i) `[1, 2]`
- (ii) `[1, [2]]`
- (iii) `[[1], 2]` [6]

(b) Define a Standard ML function *even* that takes an integer and returns *true* if and only the integer is an even number. [2]

(c) Define a Standard ML function *empty* that takes a list and returns *true* if and only if the list is empty. [2]

(d) Define a Standard ML function *triple* that takes a list of integers and multiplies each of the integers by three. For example, `triple([1, 2, 3])` should return `[3, 6, 9]`. [3]

(e) The function *f* is defined as follows:

```
fun f(nil) = 0 |  
  f(h::t) = (h * h) + f(t);
```

Give a step-by-step evaluation of `f([1, 2, 3])`. [5]

(f) Define a Standard ML function *factorialL* that takes a list *x* of integers and returns the list containing the factorials of all the elements in *x*. For example, `factorialL([3, 4, 5])` would evaluate to `[6, 24, 120]`. **Hint:** you may first wish to define a function *factorial* that takes an integer and returns its factorial. [7]

### Question 7

- (a) Define a Standard ML function *tail* that takes a list and returns the tail of that list. For example, `tail([3, 2, 1])` should return `[2, 1]`. [2]
- (b) Define a Standard ML function *greater\_than* that takes two integers and returns *true* if and only if the first integer is greater than the second. [2]
- (c) Define a Standard ML function *decrease* that takes an integer list and decreases each of the integers by 2. For example, `decrease([4, 8, 5])` should return `[2, 6, 3]`. [3]
- (d) (i) Define a Standard ML function *length* that takes a list and returns its length. For example, `length([4, 5, 6])` should return 3. [2]
- (ii) Define a Standard ML function *twice\_as\_long* that takes two lists and returns *true* if and only if the first list is twice as long as the second. For example, `twice_as_long([1, 7, 3, 8], [5, 2])` should return *true* whereas `twice_as_long([6, 9], [5, 2])` should return *false*. [3]
- (e) (i) Define a Standard ML function *product* that takes an integer list and returns the product of all the integers. For example, `product([1, 2, 3, 4])` should return 24, which is the result of  $1*2*3*4$ . [3]
- (ii) Having defined *product*, give a step-by-step evaluation of the expression:
- `product([4, 5, 6])` [4]
- (f) Suppose that we have some records about certain people, for example, one record is: `{name="bob", age=30, profession="manager", weight=150.57}`.
- (i) What is the type of this record? [2]
- (ii) Define a function *older* that takes two persons' records and return *true* if and only if the first person is older than the second person. [4]

### Question 8

- (a) What does it mean to say that Standard ML is strongly typed? [3]
- (b) (i) Explain the rules of *empty* and *add* in the following definition of a datatype, illustrating your answer by showing how such a structure containing the numbers 1, 2, 3, and 4 could be represented:
- datatype set = empty | add of int \* set; [4]
- (ii) Define a Standard ML function *front* that takes an integer  $x$  and a set  $y$  and adds  $x$  to the front of  $y$ . [2]
- (c) Define a Standard ML function *last* that takes a list of integers and returns the last integer in the list. For example, `last([1, 2, 3])` should return 3. [3]
- (d) Define a Standard ML function *squareL* that takes a list of integers and squares all the integers. For example, `squareL([1, 2, 3])` should return `[1, 4, 9]`. [3]
- (e) Define a Standard ML function *sumEven* that takes a list of integers and returns the sum of the even integers. For example, `sumEven([1, 2, 4, 7])` should return 6. [4]
- (f) Write brief notes on Polymorphism and Overloading, explaining the differences between them using *append* and `<` as examples. [6]

### Question 9

(a) What does it mean for two Prolog terms to match? In your explanation **give** the rules for matching in Prolog. [4]

(b) Determine the results of the following queries in Prolog. Explain your answers.

?- admires(john, X) = hates(Y, mary).

?- likes([pat, sue], [tom, jim, bob]) = likes(X, [Y, Z]).

[5]

(c) Define left-recursion and explain the problem it can cause. **Illustrate** your answer with an example. [5]

(d) Define a Prolog predicate *only\_two* that takes a list and returns *Yes* if and only if the list contains exactly two elements. For example, *only\_two*([a, b]) should return *Yes* whereas *only\_two*([a, b, c]) should return *No*. [2]

(e) Suppose the following have been given:

- 1) male(john).
- 2) male(steve).
- 3) female(mary).
- 4) married(john).
- 5) married(mary).
- 6) unmarried(steve).
- 7) bachelor(X):- male(X), unmarried(X).

Give a step-by-step evaluation of the following queries in terms of unification and goal replacement in the goal stack:

?- married(john).

[3]

?- bachelor(X).

[6]

### Question 10

- (a) Explain the meaning of *facts*, *rules* and *queries* in Prolog, giving suitable examples [6]
- (b) Without using the built-in operator *not*, define a Prolog predicate *different* that takes two items and returns *Yes* if and only if the two items are different. For example, *different(a, b)* should return *Yes* whereas *different(a, a)* should return *No*. [3]
- (c) Define a Prolog predicate *sum* that takes a list *L* of integers and an integer *N* and returns *Yes* if and only if the *N* is the sum of all the integers in *L*. For example, *sum([1, 2, 3], 6)* should return *Yes* while *sum([1, 2, 3], 10)* should return *No*. [3]
- (d) Define a Prolog predicate *sum2* that adds up all the **odd** integers in a list. For example, *sum2([2, 3, 4, 1], 4)* should return *Yes* while *sum2([2, 3, 4, 1], 10)* should return *No*. [4]
- (e) Explain the behaviour of the functor *not* in Prolog, and discuss the difference between *Yes/No* and *true/false* in Prolog. Illustrate your answer by considering the query `?-single(clinton)`, given the following facts and rule:

```
single(bob).  
married(ivy).  
single(X):- not (married(X)).
```

[9]