

Statistical Models of Music Cognition

Geraint A. Wiggins, Daniel Müllensiefen & Marcus T. Pearce Intelligent Sound and Music Systems Group Goldsmiths, University of London





- I. General methodology: statistical corpus-based musicology
- 2. Musical similarity
- 3. Melodic pitch expectation
- 4. Melodic segmentation
- 5. Specific methodology
- 6. Summary and future work





General metholodogy

General methodological issues



• What is music (for the purposes of this work)?





- Study music entirely as cognitive/perceptual phenomenon
 - ask whether perceptual primitives and learning together can give rise to music
- Approach based on unsupervised learning over a musical surface based on perceptual primitives
 - no hand-coded rules
 - no appeal to music theory beyond notes and intervals
- Attempt to model **low-level cognition of musical structure** at level as close to perception as possible
 - no imposed high-level structural rules
- Ockham's Razor: simple models wherever possible

- Use corpus-based methods involving large bodies of data from which generalisations can be made
 - borrow successful methods from computational linguistics
 - use theories of implicit learning
- Use general models of learning applied to specific data
 - achieve **explanatory** model where the process is explained as well as the effect (descriptive/explanatory, explanandum/explanation, final/efficient cause)
- Reuse existing models to explain further (related) effects
 - this strengthens case for original model (Popper/Honing)
 - we call this **meta-modelling** ($\mu\epsilon\tau\alpha$, Gr. beyond)

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- Apply reductionist scientific methods but in a musically realistic way
 - use music written by **real composers**
 - choose music suitable for particular enquiries and experiments
 - use **complex sound** (not sine waves)
 - **avoid artificial alterations** in music
 - maintain as **normal** a **listening environment** as possible
- In short, **maximise ecological validity**

Relation to GTTM









Melodic similarity

Models of musical memory

• Unfamiliar tune



• Memory representation after 2nd listening



• After 6th listening



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Models of musical memory

- Can we predict melodic memory?
- What is remembered?
- How does memory improve over repeated listenings?
- Which musical features enhance memory?

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Melodic similarity as a tool

- I0 subjects (740 observations)
- Rank correlation between similarity and trial number for each dimension:
 - Micro-Motives: 0.252**
 - Rhythm: 0.219**
 - Accents: 0.209**
 - Contour: 0.196**
 - Pitch: 0.14**
 - Implied harmony: .005
- Interpretations:
 - Similar learning curves for melody structure and details
 - Representation of harmonic structure depends on musical background



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- The SIMILE toolbox (Müllensiefen & Frieler, 2004, 2007):
 - Systematise, implement, and combine many suitable similarity algorithms and transformations for melodic data
 - Test algorithms against data from psychological experiment
 - Algorithms: Edit Distance, substring frequency comparisons, vector correlations and differences
 - Transformations: Interval and rhythm classification, contour, harmonic implications, accent weighting

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• SIMILE's 50 Similarity Measures

Raw pitch edit distance Raw pitch edit distance weighted Raw pitch Pears. Brav. correlation Raw pitch P-B. corr, weighted, 0-1 Raw pitch Pears. Brav. Corr. Weighted Raw pitch P-B. Corr. weighted, 0-I Raw pitch crosscorrelation Raw pitch crosscorrelation weighted Contour (Steinbeck) edit distance Contour (Steinbeck), P-B. correlation Contour (Steinbeck), P-B. corr., 0-1 Contour (Steinbeck), Crosscorrelation Contour. Edit distance Contour. Pearson-Bravais correlation Contour, Pearson-Bravais corr., 0-1 Contour. Crosscorrelation Fourier (ranks) Fourier (ranks), weighted, 0-1 Fourier (ranks), weighted Fourier (ranks), weighted, 0-1 Fourier (ranks, intervals) Rhythm (gaussified onset points) Rhythm (fuzzy, Edit distance) Accent similarity measure

Intervals (Edit distance) Intervals (Mean difference) Intervals (Mean difference, exp.) Intervals (fuzzy), Edit Distance Intervals (fuzzy contour) n-grams Sum Common (intervals) n-grams Ukkonnen (intervals) n-grans Coordinate Matching (intervals) n-grams Sum Common (interval dir.) n-grams Ukkonnen (interval dir.) n-grams Coord. Match. (interval dir.) n-grams Sum Common (fuzzy int.) n-grams Ukkonnen (fuzzy int.) n-grams Count distinct (fuzzy int.) n-grams sum common (fuzzy rhythm) n-grams Ukkonnen (fuzzy rhythm) n-grams Coord. Match. (fuzzy rhythm) Selfridge-Field (max.) Selfridge-Field (modus I) Selfridge-Field (modus II) Selfridge-Field (signs) Harmonic correlation (type I) Harmonic correlation (type II) Harmonic correlation (Edit distance) Harmonic correlation (circle)



- What is missing in SIMILE?
 - A model of experience with melodies from the real world (all previous similarity measures behave as though they had never seen a melody before)
- How to model melodic knowledge in a similarity measure?
 - Term Frequency Inverted Document Frequency (TF-IDF) measures
 - Idea: Take statistical frequency of melodic feature / formula into account when comparing melodies for feature
 - Prerequisite: Corpus of melodies that is representative for style



• Example: TF-IDF measures for substrings (interval transformation)

A rare motive

A common motive





More diagnostic, if present in two melodies $(f = 7.1 \times 10^{-5})$ Less diagnostic, if present in two melodies $(f = 4.9 \times 10^{-3})$



TF-IDF similarity for melodies s, t from corpus C: $\sigma_{C;n}(s,t) = \frac{\sum_{\tau \in s_n \cap t_n} IDF_C(\tau)(TF_s(\tau) \cdot TF_t(\tau))}{\sum_{\tau \in s_n \cap t_n} IDF_C(\tau)}$

 $TF_{(m,\tau)} = \frac{f_m(\tau)}{\sum f_m(m_n)}$

TF-IDF correlation similarity:

$$\sigma_{C;n}(s,t) = \frac{\sum_{\tau=1}^{N} TFIDF_{(s,C)}(\tau) \cdot TFIDF_{(t,C)}(\tau)}{\sqrt{\sum_{\tau=1}^{N} (TFIDF_{(s,C)}(\tau))^{2} \cdot \sum_{\tau=1}^{N} (TFIDF_{(t,C)}(\tau))^{2}}}$$

with Term-Frequency for term τ in melody m with m_n different terms:

with combined TF-IDF weighting:

$$TFIDF_{(m,C)}(\tau) = TF_{(m)}(\tau) \cdot IDF_{C}(\tau)$$

and Inverted Document Frequency for term τ in corpus C with |C| melodies:

$$IDF_{C}(\tau) = \begin{cases} \log \frac{|C|}{|m:\tau \in m|} & \exists m \in C : \tau \in m \\ \log \frac{|C+2|}{2} & else \end{cases}$$





Melodic expectation

Expectation in music



- Introduction: expectation in music
- A statistical learning account
 - theory
 - model
- Results

Expectation in music



• Implication: What happens next?



• Closure: What about here?



- Focus on:
 - monody
 - pitch (interval)

Why study expectation?



- Theoretical Perspective (Meyer)
 - aesthetic experience
 - communication of emotion and meaning
- Empirical Perspective:
 - recognition memory for music
 - production of music
 - perception of music
 - transcription of music
- Can a purely unsupervised statistical model account for observed patterns of expectation as well as other models?

The IDyOM model





- STM: n-gram (arbitrary n) model
 - complex backoff/smoothing strategy
 - dynamic weighting of features used for prediction, according to information content
- LTM: same as STM
 - but trained with a database of >900 tonal melodies

The IDyOM model



- No domain-specific a priori rules
- STM and LTM can be used independently or together
- "optimised" for pitch expectancy prediction





• Chosen to reflect a range of Western tonal musical styles:

Description	Compostions	Events	Mean event/composition
Canadian folk songs	152	8,553	56.27
Chorale melodies	185	9,227	49.88
German folk songs	566	33,087	58.46
Total	903	50,867	56.33

Method: model comparison

- Compare with two-factor+tonality model of Schellenberg (1997) against behavioural data from
 - Cuddy & Lunney (1995): single-interval context
 - Schellenberg (1996): within British folk songs
 - Manzara et al (1992): throughout chorale melodies
- Criteria (Cutting et al., 1992)
 - Scope: compare correlations with behavioural data
 - Selectivity: compare performance on random data
 - Simplicity: multiple regression analysis of nested models

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Scope	Two-factor R	IDyOM R	t-test of difference
Cuddy & Lunney (1995)	0.83	0.85	n.s.
Schellenberg (1997)	0.87	0.91	_P < 0.05
Manzara et al (1992)	0.41	0.80	P < 0.01

• IDyOM accounts for the data at least as well as the two-factor model





Melodic segmentation

Melodic segmentation

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Phrase

- (most?) important unit of melodic content
- often relates to practical musical parameters, e.g. articulation, breathing, agogics, tempo change
- **smallest melodic unit** where many features can be meaningfully computed, e.g. contour, length, complexity, event density, implied harmony
- (feature description approach in melodic similarity work depends on phrases)
- How can we segment a melody into musically meaningful phrases?
- What musical information contributes to cognitive judgements of boundaries?

Gestalt rules & models

- Strong support that perceived boundaries are influenced by:
 - the presence of rests or pauses (GPR2a)
 - the presence of notes with relatively long duration or inter-onset interval (GPR2b)
- Less definite support for other dimensions
- Many symbolic, rule-based segmentation models in literature
 - Lerdahl & Jackendoff, 1983; Deliège 1987-1997; Rowe, 1993; Friberg et al., 1998; Cambouropoulos, 1998-2008; Temperley, 2001; Ahlbäck, 2004; Weyde, 2004; etc
- A few evaluation studies published, but as phrase boundaries are in many instances not consistently given by composer, they use
 - Analytical annotations by I subject (e.g. Bod, 2001)
 - Experimentally collected ratings by several subjects (e.g. Deliège, 1987-98; Thom et al., 2001; Melucci & Orio, 2002; Spiro & Klebanov, 2006; Bruderer et al., 2008)

Segmentation from expectation



- Evidence from computational linguistics for a statistical segmentation strategy
 - Statistical learning of syllable/tone sequences (Saffran et al., 1996, 1999)
 - Predicting word boundaries in speech processing (Brent, 1999)
- Perceptual groups associated with points of closure where expectations are weak (Meyer, 1957; Narmour, 1990)
- In information theoretic terms (Shannon, 1948):
 - Uncertainty: entropy \approx information content of a probability distribution over events predicted from context
 - Unexpectedness: information content (or low probability) of an event in context

• Our hypothesis:

• Closure: increasing certainty followed by lack of certainty \approx decreasing entropy/IC followed by (relatively) high entropy/IC





- What's new here?
 - Comparing programmed Gestalt models and information theoretic segmenters
 - Explicit search for optimal hybrid model
 - Explicit distinction between items (melodies) with low/high agreement
 - Explicit search for consistent but diverging rating patterns

The models



- Gestalt, programmed-rule-based:
 - GPRs (Lerdahl & Jackendoff, 1983; Frankland & Cohen, 2004)
 - Grouper (Temperley, 2001)
 - LBDM (Cambouropoulos, 2001)
 - SimpleSegmenter (Müllensiefen & Frieler, 2004)
- Information theoretic (no programmed musical knowledge)
 - Saffran et al (1999)
 - IDyOM (now)

The method



- Subjects: 25 adults, musicology (graduate) students, mean age: 28.4 (Std: 8), mean years playing instrument: 16.4 (Std: 9), mean number of paid gigs 36.3 (Std: 60.6), mean months paid instrumental lessons: 100.8 (Std: 72.3), mean practice hours in most active musical phase: 27.4 (Std: 17.5)
- Preliminary task: Indicate phrase boundary strength (on 3-point scale) while listening; 2 consecutive listenings for each melody
- Definition of phrase boundary: end of musical segment where a performer would make phrase indication; tested in group
- Material: 15 monophonic melodies from pop or folk songs, 50-132 notes at natural tempo, MIDI piano renditions
- Questionnaire about musical background
- Dependent variables: binary indicator of majority vote





- Obtain segmentations of each of 15 melodies by human experts
- Check consistency of ratings between subjects for each melody using K measure for inter-rater agreement (Fleiss, 1971; Spiro & Klebanov, 2006)
- 7 melodies with $\kappa \ge .6$ on binary ratings ('moderate agreement', Landis & Koch, 1977) taken as reliable melodies
- 8 unreliable melodies ($\kappa < .6$) saved for later analysis
- Main Task: predict segmentation boundaries on notes where ≥ 50% of subjects agreed on boundary using segmentation algorithm
- Measures of accuracy: precision/recall; FI; d'; κ



- Hybrid model combining several algorithms into logistic regression model, using stepwise model selection (Bayes' Information Criterion)
 - Predictors (binary): IDyOM, Grouper, LDBM, SimpleSeg, Saffran, GPRs
 - Criterion (binary): majority vote
 - Model: Logistic regression
 - Variable selection by model comparison using Bayes' Information Criterion
- Optimal model:

p(boundary) =
$$\frac{1}{1 + e^{-(6.04 \cdot Grouper + 2.73 \cdot IDyOM - 5.17)}}$$

Comparing models



	Precision (1 - specificity)	Recall (sensitivity)	FI	ď	К
never	0	0	-	-	04
saffran.p.pitch	.10	.04	.06	.14	.01
always	.08	I	.15	-	86
GPR2b	.13	.19	.15	.38	.07
GPR3a	.16	.37	.22	.69	.12
SimpleSeg.	.25	.35	.29	.99	.22
IDyOM	.60	.63	.61	2.15	.58
LBDM2001	.86	.57	.69	2.61	.67
GPR2a	.95	.55	.70	2.93	.68
Grouper	.67	.87	.76	2.94	.73


- We use the IDyOM expectation model as the basis for a meta-model for predicting melodic segmentation
 - a **meta-model** uses an existing model (without changing it) to predict a different, related phenomenon
 - IDyOM uses the information-theoretic properties of the distributions generated by the pitch expectation model
- We give this simple idea a name because the existence of meta-models adds evidence for the correctness of the models on which they are based

A meta-model









Specific methodology

Analysis methodology



- 'Traditional' data analysis: 'Majority vote approach'
 - Add all subjects' boundary indications
 - Use threshold (e.g. 50%) to determine 'true' boundaries
 - Model 'true' boundaries only



- Problems with majority vote:
 - Low subject agreement on certain melody items and exclusion of melody items from dataset
 - Incomplete segmentation solutions at fixed threshold

Melody no.	Mean no. boundaries	StDev. boundaries	Boundaries at 50% agreement	% of part. req. to agree f. mean no. of boundaries	K ≥ 0.6
	6.88	4.30	6	21	-
2	9.00	3.13	7	42	+
3	4.13	I.84	3	43	-
4	8.74	3.63	4	43	-
5	9.96	2.12	8	46	+
6	9.78	3.22	9	30	+
7	3.82	1.37	I	41	-
8	10.48	3.22	10	56	+
9	9.64	2.69	10	64	+
10	4.39	1.73	3	52	-
11	9.36	3.58	7	36	-
12	7.84	1.82	8	80	+
13	3.08	1.51	I	28	-
14	9.72	3.10	8	40	+
15	11.16	4.44	9	36	-

• Problems with majority vote:

Number of participants indicating boundary

• Incomplete segmentation solutions







- Problems with majority vote:
 - No concept of multiple valid solutions



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- Alternative approach to data analysis:
 - Clustering of subjects with similar strategies
- For each melody, measure similarity between ratings of all pairs of subjects using Jaccard distance
- Project distances onto lower-dimensional space (4D) using metric MDS
- Use model-based clustering (Fraley & Raftery, 1998) to
 - determine outliers among subjects (NNclean procedure from MCLUST)
 - cluster subjects
 - decide on cluster model and number by BIC
- Compute inter-subject agreement within cluster using Fleiss' kappa (1971)

$$\kappa = \frac{P(actual) - P(expected)}{1 - P(expected)}$$



• Results: *K* values for inter-rater agreement

Melody no.	No. clusters	k cl. l	k cl. 2	k cl. 3	k cl. 4	No. part. in noise cl.
I	3	.97	.93	.82		8
2	2	.91	.72			9
3	2	.90	1.00			15
4	3	.90	.70	.88		16
5	3	.83	.83	.90		8
6	I	.90				14
7	4	.68	.62	.80	.69	I
8	2	.91	.96			17
9	4	.83	.91	1.00	1.00	9
10	4	.86	.58	.85	.63	7
11	2	.67	.69			- 11
12	2	.97	.72			9
13	4	1.00	1.00	.54	.47	14
14	4	.97	.89	.96	.80	10
15	4	.60	.64	.66	.66	3

Segmentation Clustering: Results



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- Evaluation of segmentation algorithms according to optimal clustering
 - Compute 'true' boundaries for each cluster (on each melody) by model-based clustering (2 clusters only) from aggregated data
 - For each melody compute FI-performance for each algorithm with all clusters
 - Select only highest FI-value from each melody
 - Compute average over all test items

	Mean FI	StDev. FI	
never	0	0	lies
always	.24	.05	eloc
saffran.p.pitch	.26	.17	5 melodies
GPR3a	.28	.16	_
SimpleSeg.	.29	.30	over
GPR2b	.42	.21	ince
IDyOM	.55	.28	rma
GPR2a	.56	.40	erfo
LBDM2001	.69	.18	Mean performance
Grouper	.76	.25	Ωea

		die
	Mean FI	Performance over all notes of all 15 melodie
never	0	15 n
always	.24	all
saffran.p.pitch	.24	s of
GPR3a	.28	ote
SimpleSeg.	.33	all n
GPR2b	.42	ver
IDyOM	.63	ie O
GPR2a	.75	Janc
LBDM2001	.71	form
Grouper	.79	Pert

Segmentation Clustering: Results



- Next Steps:
- Have IDyOM learn from interval and onset data
- Have IDyOM learn from different melody corpora (pop music)
- Associate subject clusters with segmentation strategies
- Combine models to build hybrid model

Part 6: Summary



I. General methodology: statistical corpus-based musicology

- I.I. Music as psychological phenomenon
- I.2. Unsupervised-learning-based models over large corpora
- 2. Musical similarity
 - 2.1. Statistical techniques to model structural similarity
 - 2.2. Need segmentation before we start
- 3. Melodic pitch expectation
 - 3.1. Learn a model from a corpus
 - 3.2. Use it to predict sequences given context
- 4. Melodic segmentation
 - 4.1. Use the information-theoretic properties of 3 in a meta-model
 - 4.2. Predict segmentation (and other musicological properties?) from statistical signals
- 5. Specific methodology
 - 5.1. How to cope with inter-subject ambiguity in human perception



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